

## 7.3 - Operational Properties I

### Theorem: First Translation Theorem

If  $\mathcal{L}\{f(t)\} = F(s)$  and  $a$  is any real number, then  $\mathcal{L}\{e^{at}f(t)\} = F(s - a)$ .

Example: Find either  $F(s)$  or  $f(t)$ , as indicated.

$$\mathcal{L}\{t^{10}e^{-7t}\}$$

$$\mathcal{L}\{e^{-2t}\cos 4t\}$$

$$\mathcal{L}^{-1}\left\{\frac{1}{s^2 + 2s + 5}\right\}$$









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If we let  $f(t) = 1$ , then we have  $\mathcal{L}\{\mathcal{U}(t - a)\} = \frac{e^{-as}}{s}$ .

**Example:** Find either  $F(s)$  or  $f(t)$ , as indicated.

$$\mathcal{L}\{(3t + 1)\mathcal{U}(t - 1)\}$$

Alternative form of the second translation theorem:

$$\mathcal{L}\{g(t)\mathcal{U}(t - a)\} = e^{-as}\mathcal{L}\{g(t + a)\}$$

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